

Hyperbolic paraboloid slice form

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A hyperbolic paraboloid is a certain surface, which is curved, but made up of straight lines, and has a saddle point.

One example of the hyperbolic paraboloid is a surface given an equation

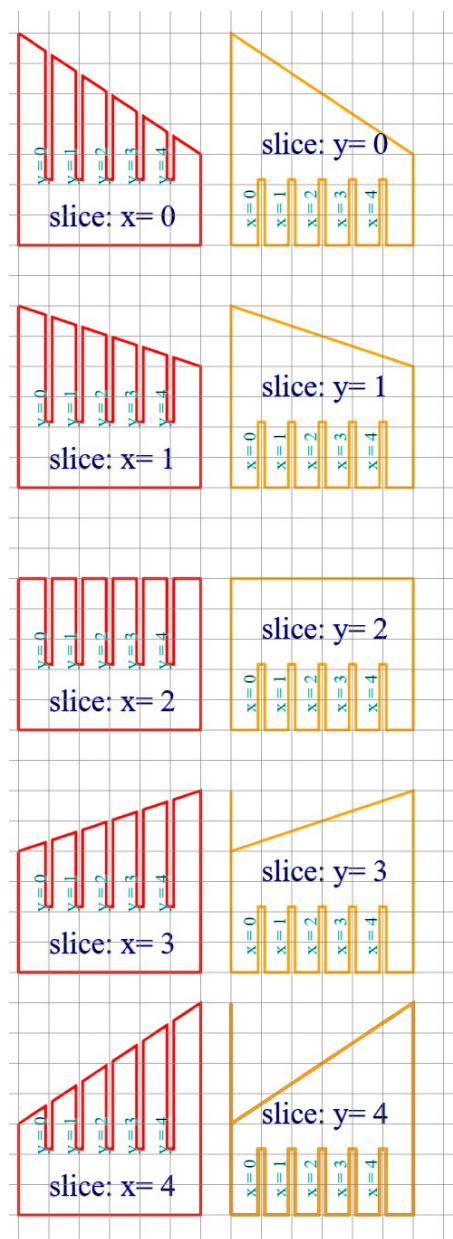
$$z = xy.$$

The point at $(0,0,0)$ is a “saddle point” - the surface curves up *and* down at this point, depending on the direction you move through the point. A Pringle crisp has approximately this shape.

A **slice form** can be used to model surfaces which can be described by equations of the form $z = f(x, y)$, like the hyperbolic parabola.

INSTRUCTIONS

- (1) Locate slices for x and y from 0 to 4, and arrange in order, as on right, for convenience.
- (2) Take $y = 0$, and slot each of the $x = 0$ to $x = 4$ slices into the slots on this side, one by one. Use a little bit of **tape** near each slot, after each is slotted together, in order to hold in place (since this model is quite small and fiddly, and otherwise falls apart easily).
- (3) Once all the $x = 0, 1, 2, 3, 4$ slices are slotted into the $y = 0$ slice, slot each of the $y = 1, 2, 3, 4$ slices into these slices. For these, you don't need to use the tape (and probably would be very difficult to use it).



(Note: with the coordinates on this page, the equation is $z = (x - 2)(y - 2)$. Thus was used to avoid confusion of negative coordinates. See over for version for $z = xy$.)

